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About the Charles A. Dana Center at The University of Texas at Austin

The Dana Center develops and scales mathematics and science education innovations to support educators, administrators, and policy makers in creating seamless transitions throughout the K–16 system for all students, especially those who have historically been underserved.

For more information about our programs and resources, see our homepage at www.utdanacenter.org

About the Dana Center Mathematics Pathways

The Charles A. Dana Center established the New Mathways Project (NMP) in 2012 as a statewide reform effort through a joint enterprise with the Texas Association of Community Colleges. As our work to support mathematics pathways expanded across multiple states, creating many opportunities for further engagement, the NMP changed its name to the Dana Center Mathematics Pathways (DCMP) to reflect this shift and the progression of our work.

For more information about the DCMP, see www.dcmathpathways.org

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