

Dana Center
Mathematics
 PATHWAYS

Co-requisite Design



The University of Massachusetts
 Charles A. Dana Center www.dcmathpathways.org

Mathematics
 PATHWAYS



Purpose
 Support mathematics faculty in designing the structure of co-requisite courses.

Audience
 Math faculty and departmental administration who are leading math pathways work.

Facilitated by
 Paula Talley
 Charles A. Dana Center

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Using this webinar

This webinar is designed to convey information and support discussion, reflection, and action.

View this webinar individually or use it with a group to structure discussion and planning. Periodically, there will be prompts for activities, including:

- Discussion/reflection
- Practice
- Plan for action

For each webinar, pause at these points as long as you wish.

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Outcomes

Participants will:

- Build on the backmapping work accomplished during and after the previous webinar.
- Understand the additional steps needed in planning the support content for a co-requisite (rather than a prerequisite) support course.
- Understand and plan for the decisions that need to be made in designing the support course structures.



Dana Center Mathematics Pathways

Dana Center Principles for Pathways

Mathematics pathways are structured so that:

- 1) All students, regardless of college readiness, enter directly into mathematics pathways aligned to their programs of study.
- 2) Students complete their first college-level math requirement in their first year of college.

Students engage in a high-quality learning experience in math pathways designed so that:

- 3) Strategies to support students as learners are integrated into courses and are aligned across the institution.
- 4) Instruction incorporates evidence-based curriculum and pedagogy.

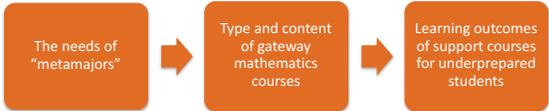


Quick Recap: Defining Content

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7

Backward mapping to define content



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8

Backward mapping to define content

For prerequisite course structures, consider carefully which skills may need to be reinforced in the college-level course or may even be best saved for initial introduction in the college-level course.

An example from a Quantitative Reasoning course is shown below.

In the college-level course, students will:	Therefore, they need the ability to:	These skills should be:		
		Taught in support course	Reinforced in college level	Taught in college level
Calculate absolute change.	Select and perform the four basic operations.	X		
Calculate relative change.	Calculate a percentage.	X		
Compare two budget categories over time.	Interpret a percentage.	X	X	
	Calculate absolute and relative change.			X

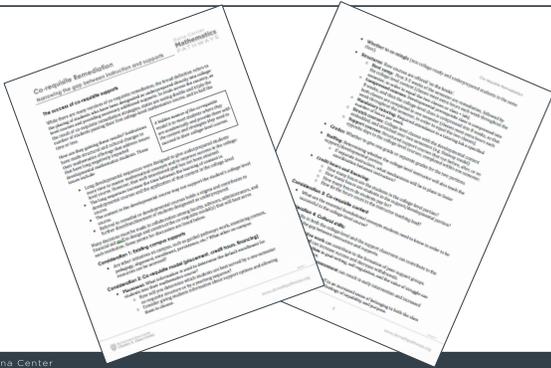
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9



Implementing Co-requisite Supports

Implementing Co-requisite Supports



Activity: Discussion/reflection



Take a few minutes to discuss with your colleagues or reflect individually:

What information did you find that resonates with you? What questions do you have?

When you are finished, proceed to the next section.

Implementing Co-requisite Supports

Co-requisite Remediation
Narrowing the gap between instruction and supports

The success of co-requisite supports

While there are many reasons for co-requisite remediation, the final decision refers to the placement of students who have been diagnosed as undergraduate directly into college-level mathematics courses. This decision is based on the results of co-requisite remediation supports. To date, the majority of the studies on co-requisite remediation supports have been positive, showing that students who receive co-requisite remediation are more likely to pass their first college-level mathematics course and to hold the title of freshman.

How are they getting these results? Institutions have made structural and cultural changes to their approaches, offering their students more and better supports. These changes include:

- Long developmental sequences were designed to give underprepared students more time to master mathematical concepts and to improve access to the college-level courses. These well-structured plans have been evaluated.
- The long sequences increase the time between the learning of content in developmental courses and the application of that content in the college-level course.
- The support in the developmental course may not support the student's collegial-level course.
- Referring to remedial or developmental courses holds a stigma and contribute to further disenfranchisement of students diagnosed as underprepared.

Many decisions must be made in collaboration among faculty, advisors, administrators, and financial aid staff. Design and implement the co-requisite model(s) that will best serve the institution's most vulnerable students.

Consideration 1: Existing campus supports

- An early intervention program such as guided pathway work, co-enrollment, tutoring, peer support, and other programs, and what other on-campus resources are available?

Consideration 2: Co-requisite model (placement, credit hours, financing)

- Placement: What information is used to determine the default placement for students in their mathematics course?
 - How will you determine which students are best served by a new semester or co-enrollment approach to the co-requisite?
 - Consider giving students information about support options and allowing them to choose.

- **Consideration 1:** Existing campus supports
- **Consideration 2:** Co-requisite model
- **Consideration 3:** Co-requisite content
- **Consideration 4:** Cultural shifts

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Implementing Co-requisite Supports

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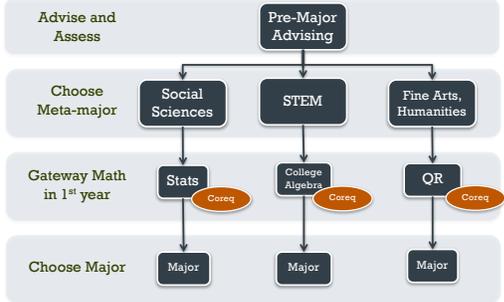
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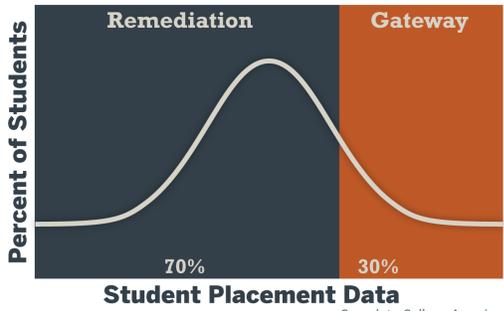
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Mathematics Pathways with Co-requisites



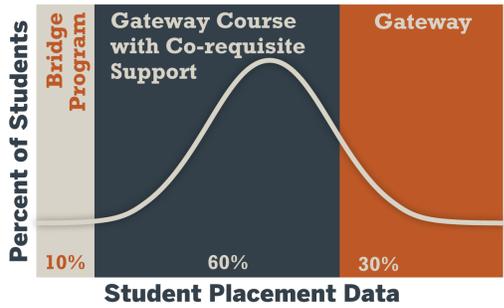
Adapted from Complete College America 2016

End Use of Traditional Placement



— Complete College America 2014

With Co-requisite, Most Students in College-Level



— Complete College America 2014

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Doubly Blended Co-requisite Model

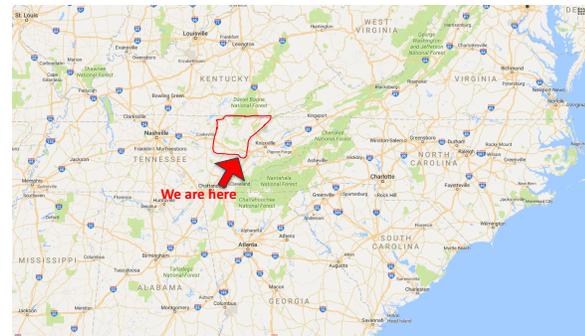


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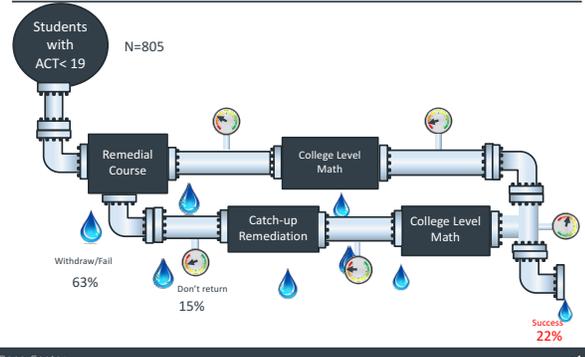
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Roane State Community College



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Leaky
Remediation Pipeline at Roane State prior to 2016



Students with ACT < 19 N=805

Remedial Course

Catch-up Remediation

College Level Math

College Level Math

Withdraw/Fail 63%

Don't return 15%

Success 22%

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Revised Model: The Co-requisite Approach

Students with ACT < 19 N = 564

MATH 1530 & MATH 0530

Withdraw/Fail 42 %

Success! 58%

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The Co-requisite Approach: Placement

- All high school students in Tennessee take the ACT test.
- This test is used for placement purposes.
- ACT Scores or <19 in math (or equivalent Accuplacer score) are required to take Co-requisite course

College Course

ACT 19+

MATH 1530 Probability and Statistics (3 cr.)

Co-requisite Course

ACT < 19

MATH 1530 Probability and Statistics (3 cr.)
+
MATH 0530 Statistical Principles (3 cr.)

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The Co-requisite Approach: Doubly Blended Model

- Each section of the college-level "Probability and Statistics" course contains students with and without learning support needs (*blended approach*).
- Students with remedial needs choose any section of the co-requisite support "Statistical Principles" course (*doubly blended approach*).
- Each section of either course may be taught by different faculty

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The Co-requisite Approach: Grading

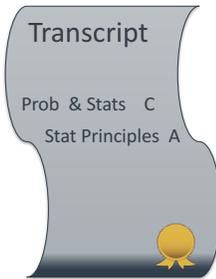
Students earn separate grades in the two courses.
Each course uses different assignments.

Probability and Stats

- 4 Tests
- 1 Final Exam
- Homework

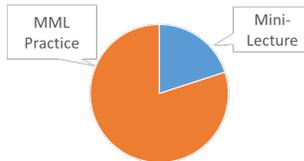
Statistical Principles

- Quizzes
- Homework
- Calculator Exercises
- Class Participation



The Co-requisite Approach: Curriculum & Instruction

- The two courses proceed in lockstep.
 - A common course calendar prescribes which topics to cover in each class period.
- Topics in the Statistical Principles learning support section are timed and structured to provide the learning support exactly when needed.
- Statistical Principles instructors are provided with a lesson plan for a mini-lecture, worksheet and guided assignments in MyMathLab



The Co-requisite Approach: Challenges



Activity: Discussion/reflection



Take a few minutes to discuss with your colleagues or reflect individually:

- What did you hear that you want to capture in your notes?

When you are finished, proceed to the next section.

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Accelerated Co-Requisite Cohort

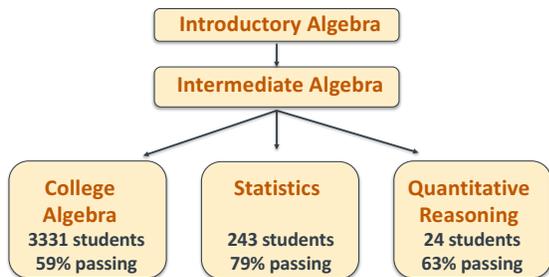
SHARON SLEDGE
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Traditional Model: No Acceleration

Fall 2015 – Fall 2016

Two Developmental Math Courses:



New Model: Accelerated Co-requisite Cohort Approach
Fall 2015 – Fall 2016

No Independent Developmental Math Course

Accelerated College Algebra (AIM) 920 students 74% passing	Accelerated Statistics (ASAP) 96 students 75% passing	Accelerated Quantitative Reasoning (AQR) 87 students 90% passing
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What is an "Accelerated Co-Requisite Cohort"?
Accelerated Quantitative Reasoning

Developmental Math Course
Math 0332

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What is an "Accelerated Co-Requisite Cohort"?
Accelerated Quantitative Reasoning

Quantitative Reasoning
Math 1332

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What is an "Accelerated Co-Requisite Cohort"?

Accelerated Quantitative Reasoning

*Accelerated
Quantitative
Reasoning
(AQR)*

*Two Courses – Two Teachers
(Support included "Just in Time")*



What is an "Accelerated Co-Requisite Cohort"?

*Accelerated Quantitative Reasoning
(AQR)*

Math 0332 & Math 1332

*Developmental
Students*

*Not College Ready
(Determined by State Placement Exam)*

Complete BOTH Courses (Remedial and Academic) in ONE Semester



Co-requisite: Accelerated Quantitative Reasoning

Curriculum and Instruction

Scissor Game
Watch/Observe
Listen
Participate
Collaborate



Course Structure
Videos/Demos
Presentations
Activities
Community



Co-requisite: Accelerated Quantitative Reasoning
Curriculum, Instruction & Assessment



Co-requisite: Accelerated Quantitative Reasoning
Curriculum

- 1 Sets & Logic
- 2 Probability
- 3 Math Finance
- 4 Geometry & Art
- 5 Statistics

Co-requisite: Accelerated Quantitative Reasoning
Instruction

Variety of presentation types

- Presentations/Lectures/Videos – by teachers/students/internet
- Discovery lessons/flipped experiences
- Technology – Excel; Graphing calculators
- Active learning – reading writing, discussing, problem solving, experiments, etc.

Co-requisite: Accelerated Quantitative Reasoning

Instruction and Assessment

Variety of presentation types

- Presentations/Lectures/Videos – by teachers/students/internet
- Discovery lessons/flipped experiences
- Technology – Excel; Graphing calculators
- Active learning – reading writing, discussing, problem solving, experiments, etc.

Assessments – formative and summative

- Module Projects
- Homework from textbook
- Module Exams/Final Exam
- Tickets in/out the door
- Capstone Project for the Course



Co-requisite: Accelerated Quantitative Reasoning

Challenges

Students

- Motivation
- Learning disabilities/Math anxiety
- FT = Face-2-Face and PT = Hybrid

Teachers

- Support/Instruction – everyday
- Keep the goal of success in front – everyday
- It takes a village – so create one
- Two are better than one but not absolute necessity



Activity: Discussion/reflection



Take a few minutes to discuss with your colleagues or reflect individually:

- What did you hear that you want to capture in your notes?
- What did you hear from Markus and Sharon that resonated with you? What questions do you still have?

When you are finished, proceed to the next section.

Activity: Discussion/reflection



Take a few minutes to discuss with your colleagues or reflect individually:

- What are the pros and cons of creating cohorts of underprepared students?
- What are the pros and cons of co-mingling college-ready and underprepared students?

When you are finished, proceed to the next section.

Vocabulary – Calendar Structures

Just-in-time supports

Support courses: Separate, structured support courses that run before, after, or on opposite days to the college-level courses.

Embedded supports: College-level classes with the developmental content embedded.

Mandatory tutoring: Required attendance in a tutoring lab for a specified number of hours per week.

Prerequisite supports + college-level; one semester

Boot camp: First 3-5 weeks of the semester are remediation, followed by the college-level content.

Compressed courses: Developmental prerequisite class is compressed into 8 weeks, and then the college-level class is compressed into 8 weeks, so that both classes are completed in one semester.

Just-in-time supports; two semesters

Stretch courses: College-level classes with the developmental content embedded and stretched over two semesters (e.g. Statway model).

Activity: Discussion/reflection



Take a few minutes to discuss with your colleagues or reflect individually:

- What are the pros and cons of each calendar structure?

When you are finished, proceed to the next section.

Implementing Co-requisite Supports

Co-requisite Remediation
Narrowing the gap between instruction and support

The success of co-requisite supports

While there are many reasons for co-requisite remediation, the broad definition refers to the placement of students who have been diagnosed as college-prepared directly into college-level courses with parallel remedial supports. This can occur through an array of co-requisite remediation programs, such as writing labs and extra credit modules or courses, or through co-requisite support courses and lab courses.

As we are gathering these results, institutions have made structural and cultural changes to their operations to address their challenges. Here are the key findings:

- Long developmental sequences were designed to give underprepared students more time to master mathematical concepts and improve success in the college-level course. However, the cost associated with this approach is high.
- The long sequences increase the time between the learning of content in developmental courses and the application of that content in the college-level course.
- The content in the developmental course may not support the student's college-level course.
- Referral to remedial or developmental courses holds students and contributes to better development of students registered in college courses.

More decisions must be made in collaboration among faculty, advisors, administrators, and financial aid staff to design and implement co-requisite models that will best serve the needs of students who are in need of remediation.

Consideration 1: Building campus support

- An early remediation program that includes additional work, co-enrollment, tutoring, peer support, and other supports, such as writing labs, peer support, and other on-campus resources, can be successful.

Consideration 2: Co-requisite model placement, credit hours, financing

- **Placement:** What information is used to determine the student's placement in the first mathematics course?
 - How do we determine which students are best served by a co-requisite model structure in the first semester?
 - Consider giving students information about support options and allowing them to choose.

- **Consideration 1:** Existing campus supports
- **Consideration 2:** Co-requisite model
- **Consideration 3:** Co-requisite content
- **Consideration 4:** Cultural shifts

Backward mapping to define content

For prerequisite course structures, consider carefully which skills may need to be reinforced in the college-level course or may even be best saved for initial introduction in the college-level course.

An example from a Quantitative Reasoning course is shown below.

In the college-level course, students will:	Therefore, they need the ability to:	These skills should be:		
		Taught in support course	Reinforced in college level	Taught in college level
Calculate absolute change.	Select and perform the four basic operations.	X		
Calculate relative change.	Calculate a percentage.	X		
	Interpret a percentage.	X	X	
Compare two budget categories over time.	Calculate absolute and relative change.			X

Planning Co-requisite Content

Introduction to Statistics and Co-requisite Support Course Sample Timeline
Adapted from and with thanks to Roane State Community College

Day	Co-requisite Notebook Topics	On-line Lab	Essentials of Statistics Triaia 5 th ed.	MyLabs Plus! Assignment
0	Orientation, study skills, time management	0	Orientation	0
1	Whole numbers: place value, rounding, estimating, problem solving, variable expressions	1	1.1 - 1.2	Orientation; introduction to statistical terms and statistical thinking
2	Must have TI-83/84 calculator! Exponents, square roots, fractions, order of operations	2	1.3 - 1.4	Types of data; collecting sample data
3	Decimals, ratios, percent, conversions	3	2.2 - 2.3	Frequency distributions; histograms
4	Applications of percent	4	2.4	Graphs that enlighten and graphs that deceive
5	Operations on real numbers, scientific notation	5	3.2	Measures of center
6	Review of types of data, sampling methods, types of graphs	6	3.3 - 3.4	Measures of variation; measures of relative standing and boxplots
7	Review of measures of center and variation	7	Practice Test 1	
8	Comprehensive review of chapters 1 - 3 & basic skills	8	Test 1	

Activity: Discussion/reflection



Take a few minutes to discuss with your colleagues or reflect individually:

- What do you notice about the Roane State calendar?
- What questions do you have?

When you are finished, proceed to the next section.

Planning Co-requisite Content

15	Area of a rectangle, lower/upper boundaries of regions, identify specified area under a curve, shade the area representing a percentile	15	6.2 - 6.3	Standard normal distribution; applications	11
16	Uniform distribution, standard normal curve, find z-scores, find critical values, determine type of problem	16	6.5	Central Limit Theorem	12
17	Probability/proportion/percent, calculate critical values, deconstruct intervals, identify parts of proportion problems	17	7.2	Estimating a population proportion	13
18	Find the best point estimate, calculate CI estimate for proportion, determine the required sample size	18	7.3	Estimating a population mean	14
19	Review of normal probability distributions and confidence intervals	19	Practice Test 3		
20	Comprehensive review: chapters 6 - 7 and basic skills	20	Test 3		
21	Coordinate system, intercepts, graph lines, compare & round decimals	21	8.2	Basics of hypothesis testing	15
22	Slope from graph & points, average rate of change, β , s and n	22	8.3	Testing a claim about a proportion	16
23	Concepts of slope and analyzing linear relationships	23	8.4	Testing a claim about a mean	17
24	Scattergrams and concepts of linear equations	24	10.2 - 10.3	Correlation; regression	18

Activity: Plan for action

Create a plan for designing the structures of support courses for underprepared students. Plan for how you will:

- Move forward to address the four considerations and the subcategories within each.

When you are finished, proceed to the next section.

Resources available

The Dana Center Mathematics Pathways Resource site, www.dcmathpathways.com:

- **Learn About:** Essential ideas and resources targeted for essential stakeholders
- **Take Action:** Action steps and resources for institutional and classroom implementation
- **Resources:**
 - *The Case for Math Pathways*
 - *The Program of Study Briefs*
 - Videos of student and faculty sharing their experiences

Contact information

- General information about the Dana Center
www.utdanacenter.org
- Dana Center Mathematics Pathways Resource Site
www.dcmathpathways.org
- To receive monthly updates about the DCMP, contact us at
dcmathpathways@austin.utexas.edu

About the Dana Center

The **Charles A. Dana Center** at The University of Texas at Austin works with our nation's education systems to ensure that every student leaves school prepared for success in postsecondary education and the contemporary workplace.

Our work, based on research and two decades of experience, focuses on K–16 mathematics and science education with an emphasis on strategies for improving student engagement, motivation, persistence, and achievement.

We develop innovative curricula, tools, protocols, and instructional supports and deliver powerful instructional and leadership development.
